

## Warm Up

1. What is the slope of the segment with endpoints at  $(-7, 4)$  and  $(4, -7)$ ?

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{-7 - 4}{4 - -7} = \frac{-11}{11}$$

$$\frac{-11}{11} = -1$$

2. Add:  $\begin{bmatrix} 5 & -3 \\ 2 & 0 \end{bmatrix} + \begin{bmatrix} -7 & 9 \\ -1 & 6 \end{bmatrix}$

$$\begin{bmatrix} -2 & 6 \\ 1 & 6 \end{bmatrix}$$

$$2 \times 2 \quad 2 \times 3$$

3. Multiply:  $\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 6 & -2 & 1 \\ 3 & 4 & 7 \end{bmatrix}$

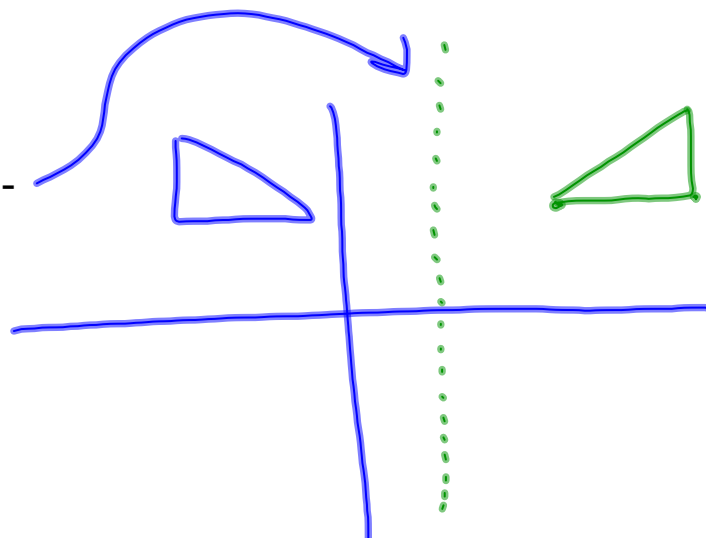
$$\begin{bmatrix} -6 & 2 & -1 \\ 3 & 4 & 7 \end{bmatrix}$$

*[Handwritten signature]*

## 9-3 Reflections

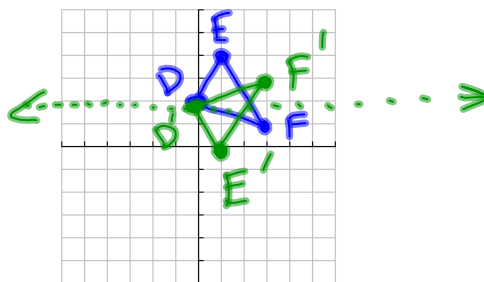
Reflection - Flip

Line of reflection -

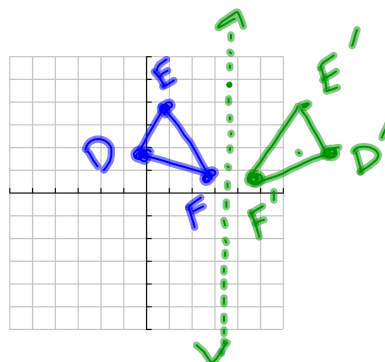


Ex 1 The vertices of triangle  $DEF$  are  $D(0, 2)$ ,  $E(1, 4)$ , and  $F(3, 1)$ . Graph the reflection described.

in the line  $y=2$   
horizontal  
 $y=2$



in the line  $x=4$   
 $x=4$

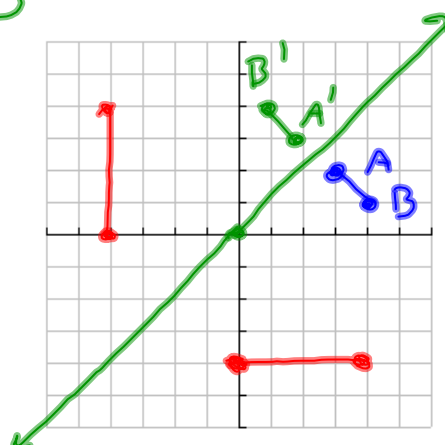


Ex 2 The endpoints of  $\overline{AB}$  are  $A(3, 2)$  and  $B(4, 1)$ . Reflect the segment in the line  $y=x$ .

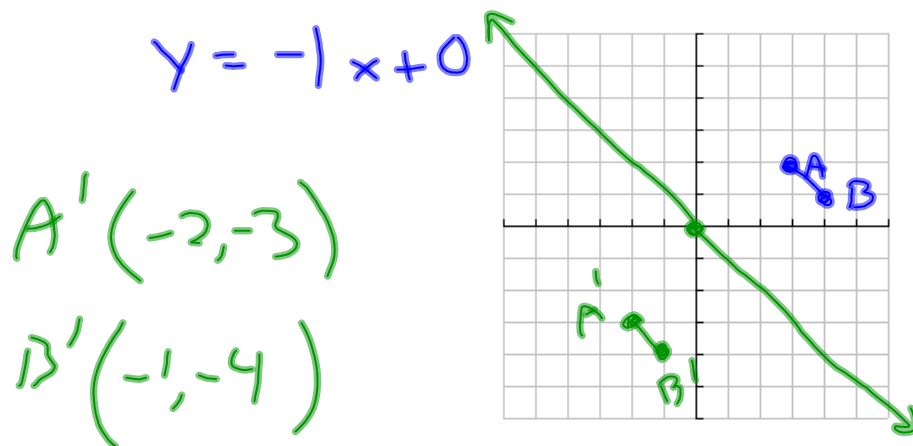
$$y = -1x + 0$$

$$A'(2, 3)$$

$$B'(1, 4)$$



Ex 3 Reflect  $\overline{AB}$  in the line  $y = -x$ .  
The endpoints of  $\overline{AB}$  are  $A(3, 2)$  and  $B(4, 1)$



### Reflection and Rotation Matrices

Reflect across the  $x$ -axis: multiply by  $\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$

Reflect across the  $y$ -axis: multiply by  $\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$

Rotate 90 degrees: multiply by  $\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$

Rotate 180 degrees: multiply by  $\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$

Rotate 270 degrees: multiply by  $\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$

Rotate 360 degrees: multiply by  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

Ex 4 Triangle  $PQR$ :  $(-3, 6)$   $(-5, 3)$   $(-1, 2)$

Reflect this across the  $y$ -axis

$$\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} -3 & -5 & -1 \\ 6 & 3 & 2 \end{bmatrix} = \begin{bmatrix} 3 & 5 & 1 \\ 6 & 3 & 2 \end{bmatrix}$$

$\underbrace{\hspace{10em}}_{2 \times 2}$ 
 $\underbrace{\hspace{10em}}_{3 \times 3}$

Ex 5 Triangle  $RST$ :  $(-1, 1)$   $(-3, 3)$   $(-4, 2)$

Reflect this across the  $x$ -axis

$$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} -1 & -3 & -4 \\ 1 & 3 & 2 \end{bmatrix} = \begin{bmatrix} \phantom{-1} & \phantom{-3} & \phantom{-4} \\ \phantom{1} & \phantom{3} & \phantom{2} \end{bmatrix}$$

Ex. 6 The vertices of  $\triangle ABC$  are  $A(5, 3)$ ,  $B(2, 8)$ , and  $C(1, 1)$ .

Reflect  $\triangle ABC$  in the  $y$ -axis.

Then reflect  $\triangle A'B'C'$  in the line  $y = 2$ .

