

p. 433

6-3 UNIT VECTORS

Properties of Vectors - p.428

$$\mathbf{u} + \mathbf{v} = \mathbf{v} + \mathbf{u}$$

$$(\mathbf{u} + \mathbf{v}) + \mathbf{w} = \mathbf{u} + (\mathbf{v} + \mathbf{w})$$

$$\mathbf{u} + \mathbf{0} = \mathbf{u}$$

$$\mathbf{u} + -\mathbf{u} = \mathbf{0}$$

$$c(d\mathbf{u}) = (cd)\mathbf{u}$$

$$(c + d)\mathbf{u} = c\mathbf{u} + d\mathbf{u}$$

$$c(\mathbf{u} + \mathbf{v}) = c\mathbf{u} + c\mathbf{v}$$



$$1(\mathbf{u}) = \mathbf{u}$$

$$0(\mathbf{u}) = \mathbf{0}$$

$$\|c\mathbf{v}\| = |c|\|\mathbf{v}\|$$

Unit vector - vector of magnitude 1

$$\mathbf{u} = \frac{\mathbf{v}}{\|\mathbf{v}\|}$$

Standard unit vectors: $i = \langle 1, 0 \rangle$ 
 $j = \langle 0, 1 \rangle$ 

So $\langle 5, -3 \rangle = ?$ $5i - 3j$

Ex 1 Find a unit vector in the direction of $v = \langle 3, -8 \rangle$

$$\|v\| = \sqrt{3^2 + (-8)^2}$$

$$= \sqrt{9 + 64}$$

$$\sqrt{73}$$

Unit vector = $\left\langle \frac{3}{\sqrt{73}}, \frac{-8}{\sqrt{73}} \right\rangle$

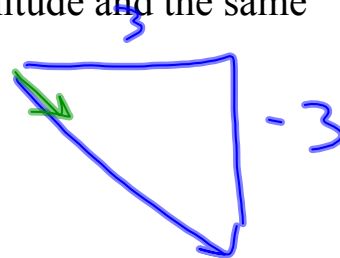


Ex 2 Find a unit vector in the direction of $v = \langle 4, -3 \rangle$

$$\text{Unit vector} = \left\langle \frac{4}{5}, -\frac{3}{5} \right\rangle$$

Ex 3 Find the vector v with the given magnitude and the same direction as u

$$\|v\| = 4 \quad u = \langle 3, -3 \rangle$$



$$\begin{aligned} \|u\| &= \sqrt{3^2 + (-3)^2} \\ &= \sqrt{9+9} \\ &= \sqrt{18} \\ &= 3\sqrt{2} \end{aligned}$$

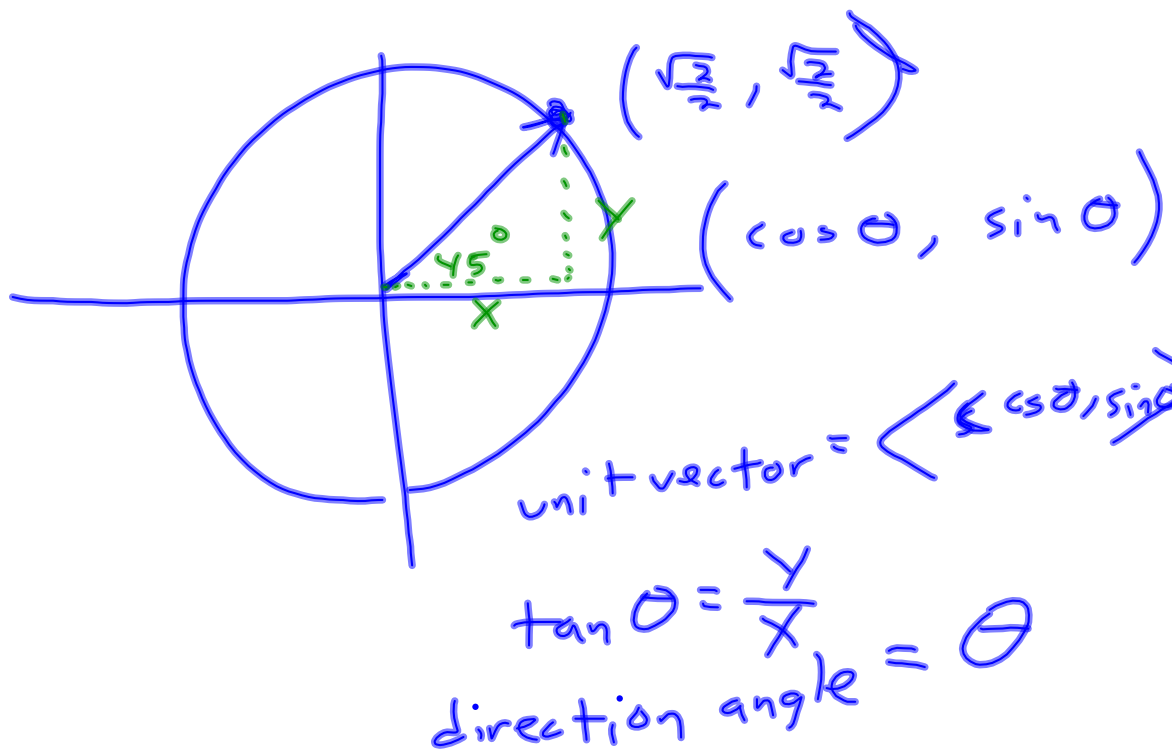
$$\begin{aligned} \text{Unit vector} &= \left\langle \frac{3}{3\sqrt{2}}, \frac{-3}{3\sqrt{2}} \right\rangle \\ &= \left\langle \frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}} \right\rangle \end{aligned}$$

$$\left\langle \frac{4}{\sqrt{2}}, -\frac{4}{\sqrt{2}} \right\rangle$$

Ex 4 Find the vector \mathbf{v} with the given magnitude and the same direction as \mathbf{u}

$$\|\mathbf{v}\| = 3 \quad \mathbf{u} = \langle 2, 5 \rangle$$

How does this relate to the unit circle?



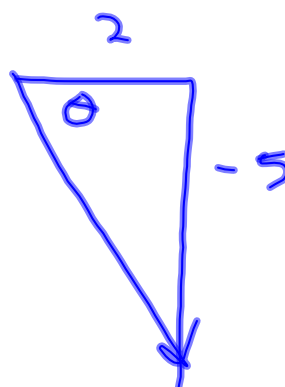
Ex 5 Find the magnitude and direction angle of

$$v = 2i - 5j \quad \text{or} \quad v = \langle 2, -5 \rangle$$

$$\begin{aligned} \|v\| &= \sqrt{2^2 + (-5)^2} \\ &= \sqrt{29} \end{aligned}$$

$$\tan \theta = \frac{-5}{2}$$

$$\theta \approx -68.2^\circ$$



Ex 6 Find the magnitude and direction angle of

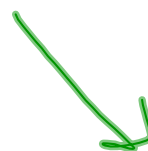
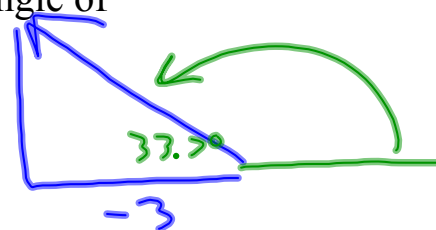
$$v = -3i + 2j \quad \text{or} \quad v = \langle -3, 2 \rangle$$

$$\|v\| = \sqrt{13}$$

$$\tan \theta = \frac{2}{-3}$$

$$\theta \approx -33.7^\circ$$

$$\theta \approx 146.3^\circ$$

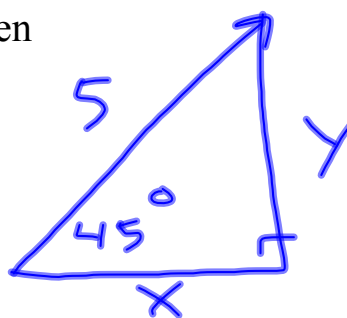


Ex 7 Find the component form of \mathbf{v} given
 $\|\mathbf{v}\| = 5$ and $\theta = 45^\circ$

$$\cos 45^\circ = \frac{x}{5}$$

$$x \approx 3.5$$

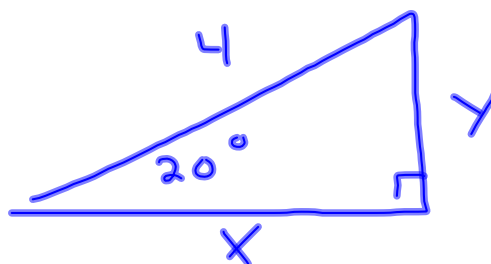
$$\langle 3.5, 3.5 \rangle$$



Ex 8 Find the component form of \mathbf{v} given
 $\|\mathbf{v}\| = 4$ and $\theta = 20^\circ$

$$\sin 20^\circ = \frac{y}{4}$$

$$\cos 20^\circ = \frac{x}{4}$$



$$\langle 3.8, 1.4 \rangle$$

Homework
p.434
#35-53, 63-69 odds